

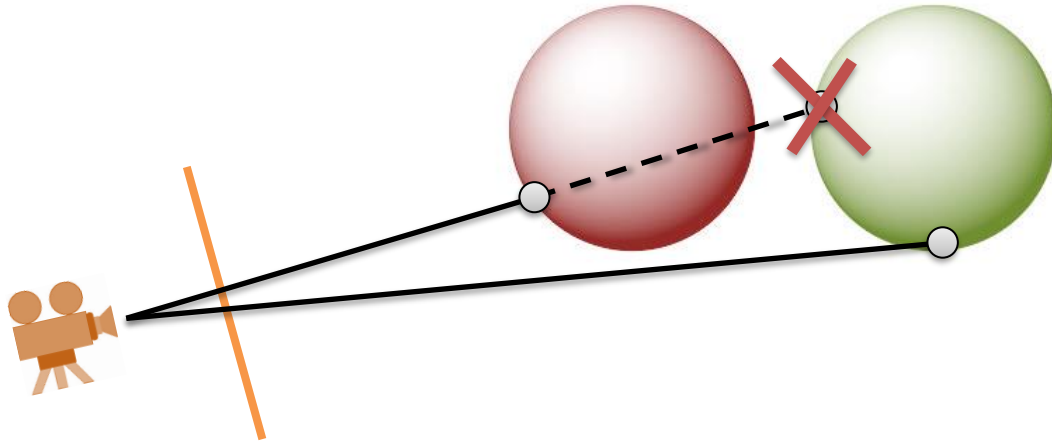
# Visibility and Shadows

Prof. Dr. Markus Gross



# Visibility

- The visibility problem
  - Some parts of some surfaces are occluded



# Visibility

- Solution 1: Painter's algorithm
  - Render objects/polygons from furthest to nearest

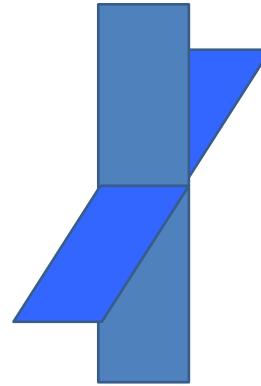


# Visibility

- Solution 1: Painter's algorithm
  - Problems



Cyclic Overlaps



Intersections

# Visibility

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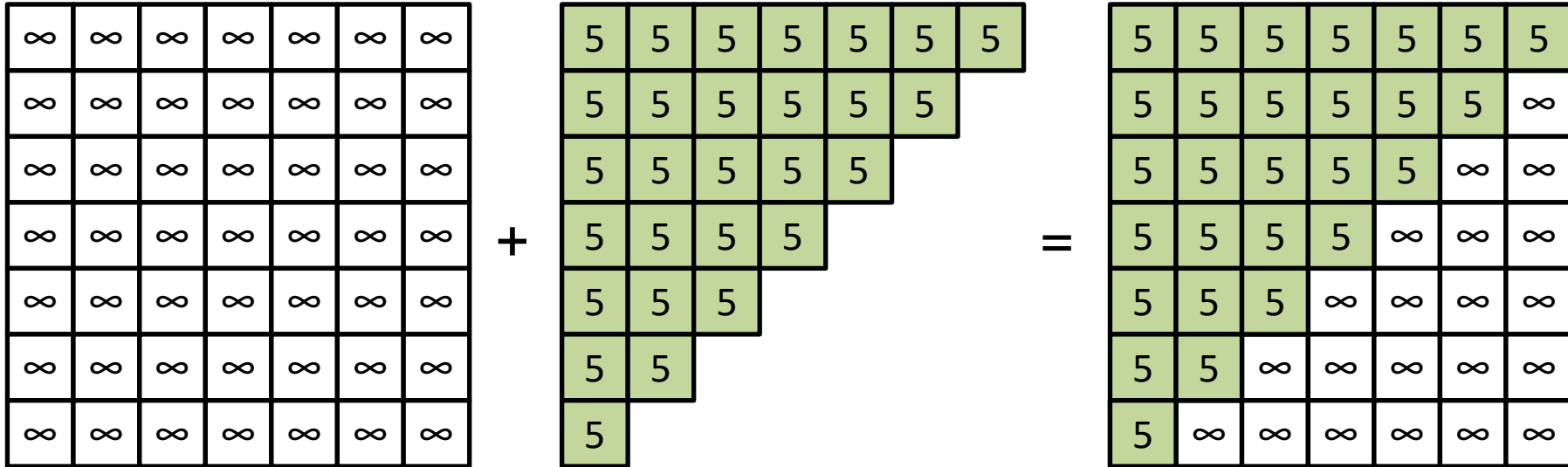
- Solution 2: Z-Buffering
  - Store depth to the nearest object for each pixel

# Visibility

- Solution 2: Z-Buffering - algorithm
  1. Initialize all z values to  $\infty$
  2. For each polygon
    - If z value of a pixel for this polygon is smaller than the stored z value, replace the stored z value

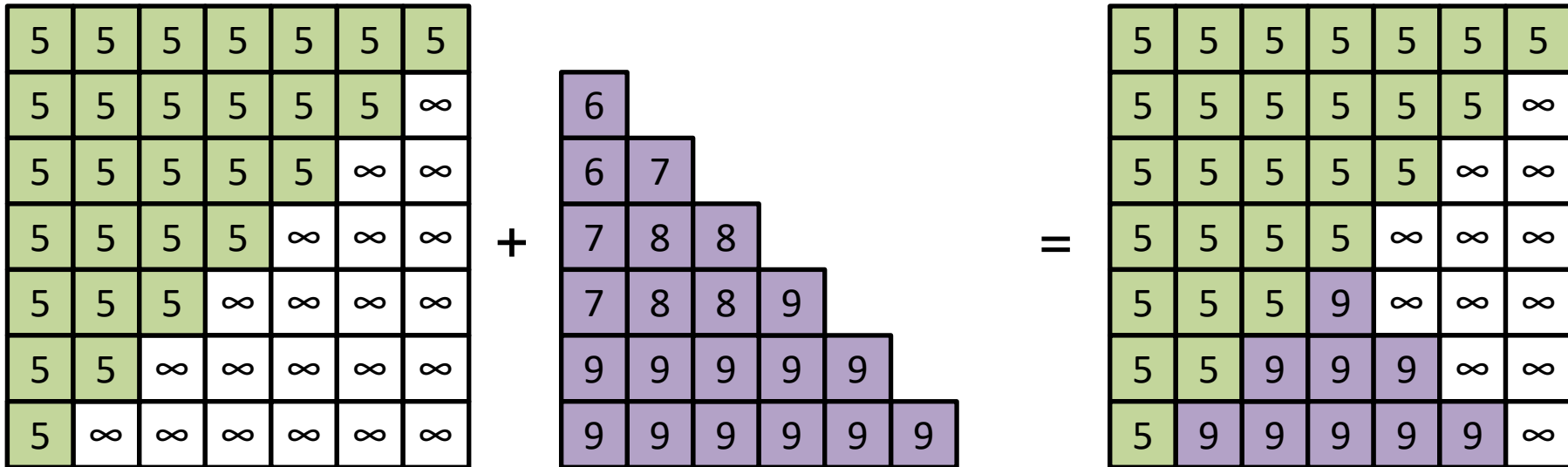
# Visibility

- Solution 2: Z-Buffering - algorithm



# Visibility

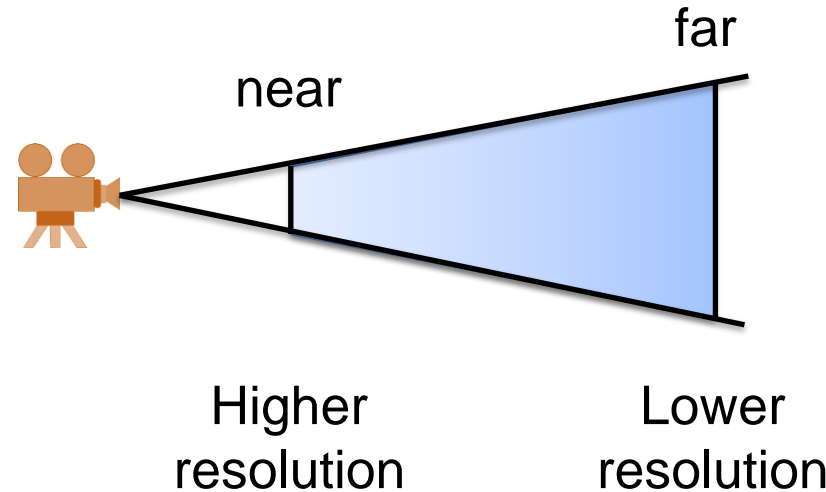
- Solution 2: Z-Buffering - algorithm





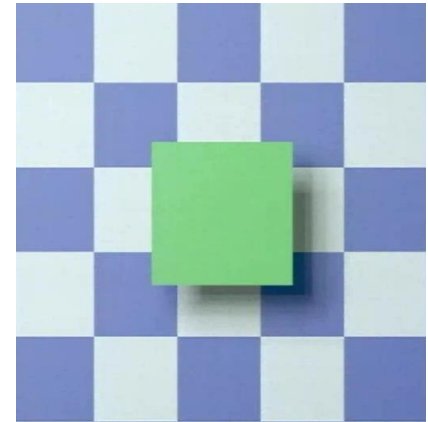
# Visibility

- Solution 2: Z-Buffering
  - Problem: limited resolution
  - Resolution is non-linear
  - Set near plane far from the camera



# Shadows

- Why are shadows important?
  - Depth cue



# Shadows

- Why are shadows important?
  - Scene lighting

Light Position



Point vs. Area Light



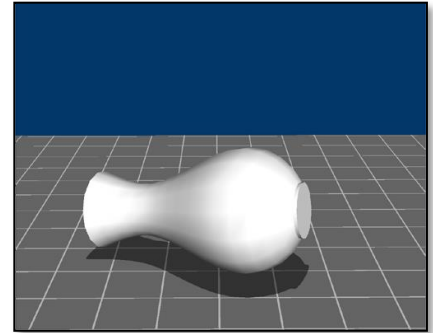
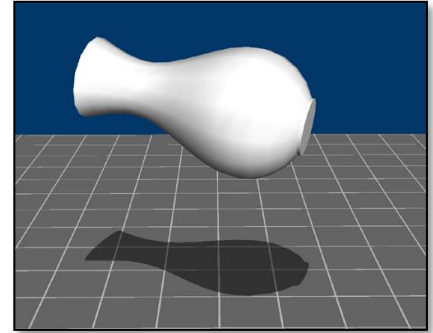
# Shadows

- Why are shadows important?
  - Realism



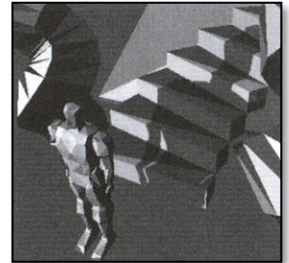
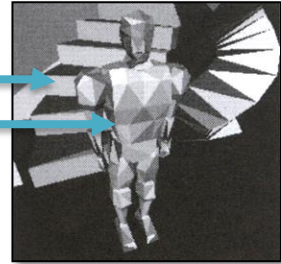
# Basic Shadows

- Planar shadows
  - Draw projection of the object on the ground
  - Limitations
    - Self shadows
    - Shadows on other objects
    - Curved surfaces



# Basic Shadows

- Projective texture shadows
  - Separate obstacle and receiver
  - Compute b/w image of the obstacle from light
  - Use image as projective texture
  - Limitations
    - Need to specify obstacle & receiver
    - No self-shadows



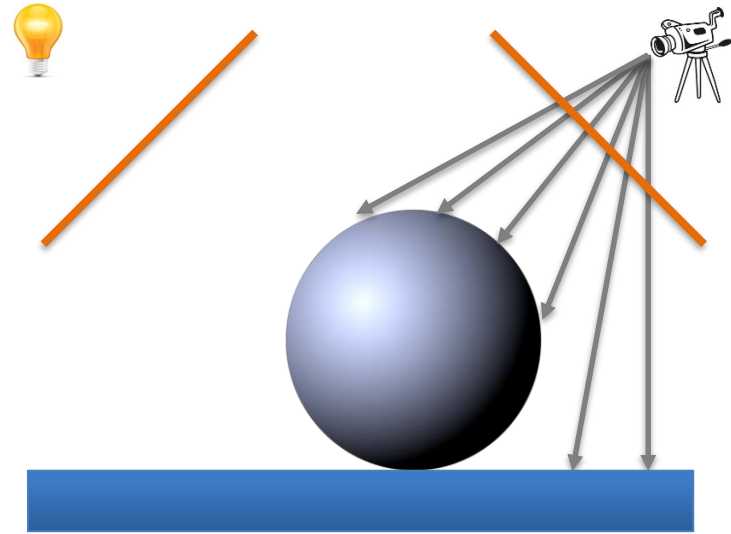
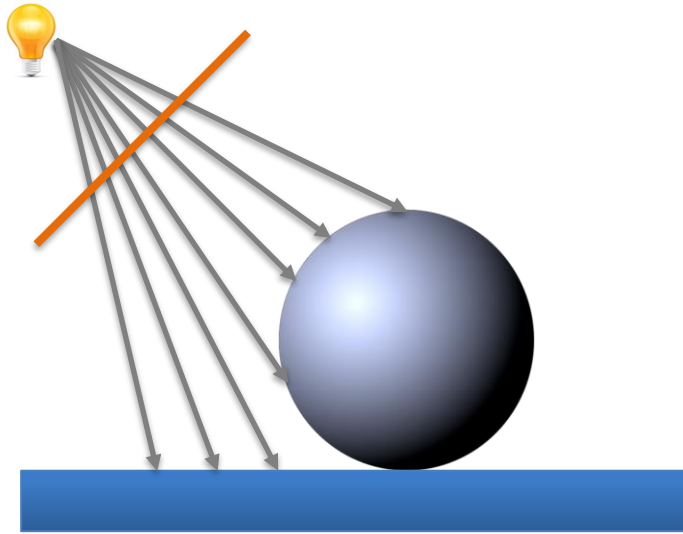
# Shadow Maps

- In high-end production software and games



# Shadow Maps

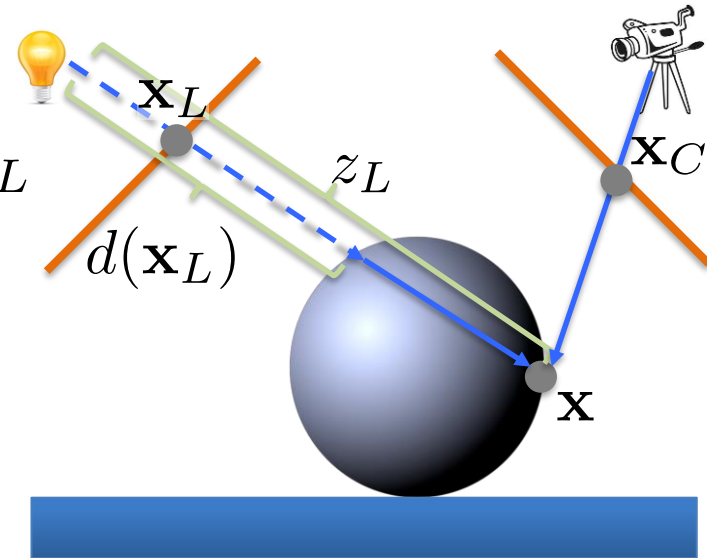
- Compute the depths from the light
- Compute the depths from the camera





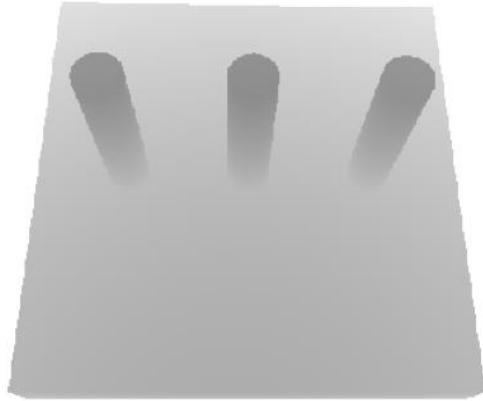
# Shadow Maps

- For each pixel on the camera plane
  - Compute the point in world coordinates
  - Project point onto the light plane
  - Compare  $d(\mathbf{x}_L)$  (shadow map) and  $z_L$
  - If  $d(\mathbf{x}_L) < z_L$ ,  $\mathbf{x}$  is in shadow

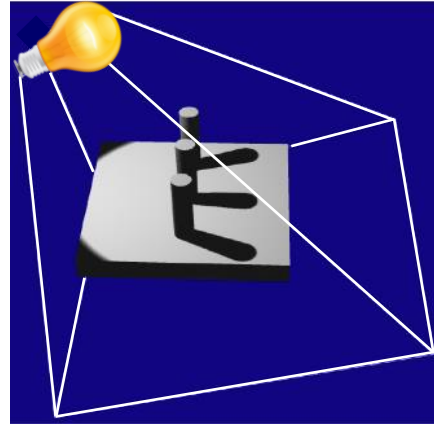


# Shadow Maps

Depth map rendered  
from the light



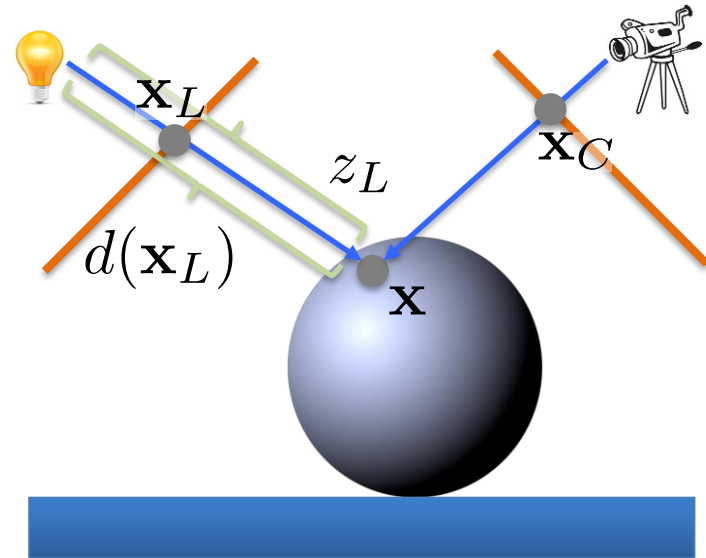
Rendering  
from the camera



# Shadow Maps

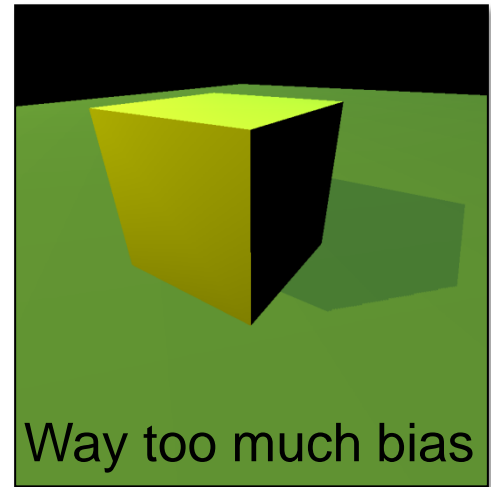
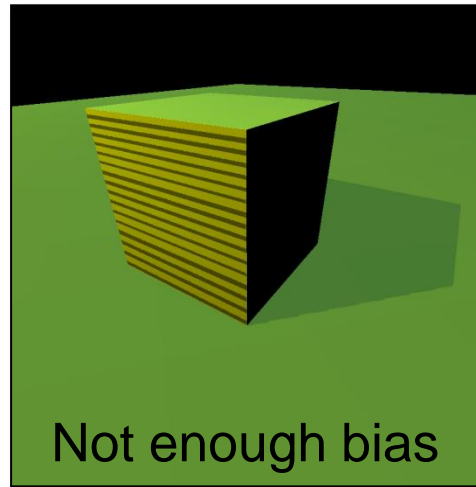
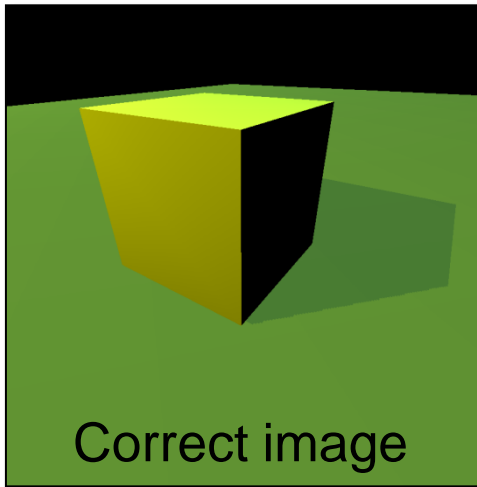
- Limitations – Bias
  - For a visible point  $d(\mathbf{x}_L) < z_L$
  - How to avoid self-shadowing?
  - Add bias

$$d(\mathbf{x}_L) + \textit{bias} < z_L$$



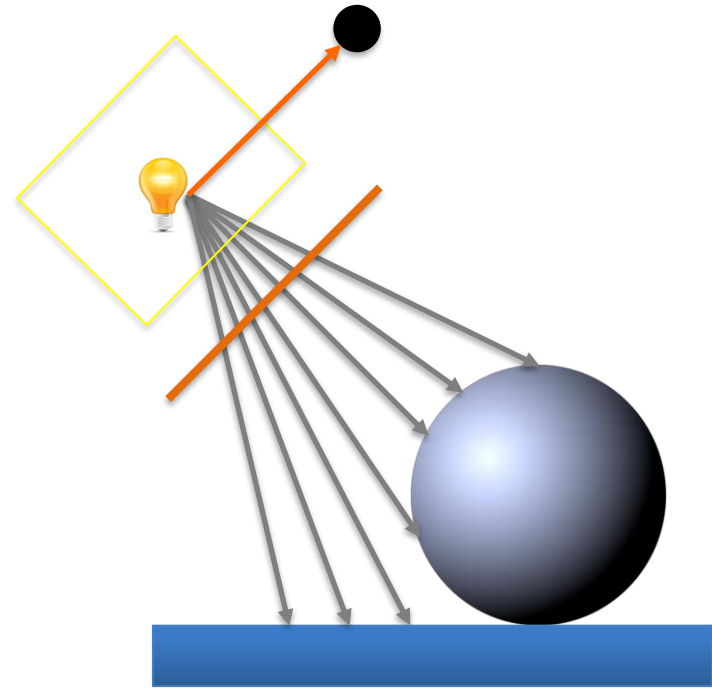
# Shadow Maps

- Limitations – Bias  $d(\mathbf{x}_L) + bias < z_L$ 
  - Choosing a good bias can be very tricky



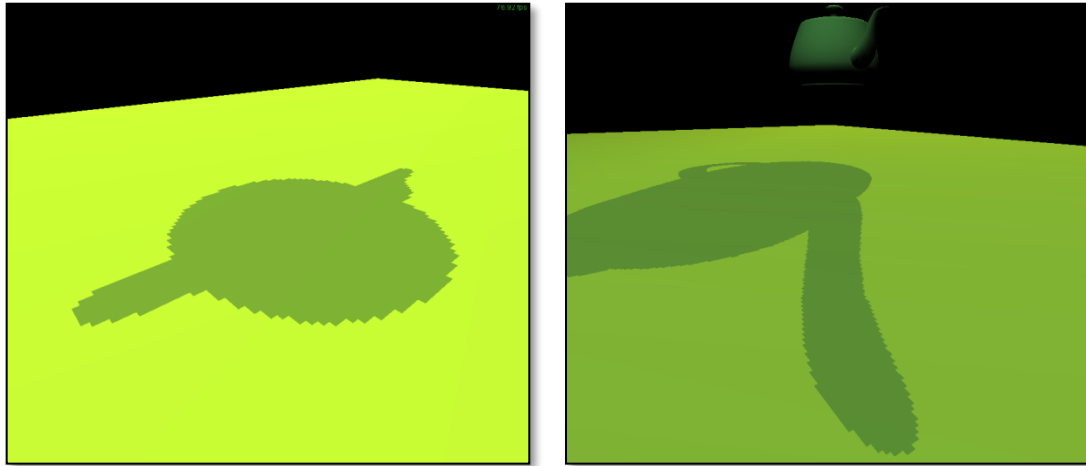
# Shadow Maps

- Limitations – Field of view
  - A point to shadow can be outside the field of view of shadow map
  - Use cubical shadow map or spot lights



# Shadow Maps

- Limitations – Aliasing
  - Undersampling of the shadow map



# Shadow Maps

- Filtering

- Should we filter depth? No.
- Instead, filter the result of the test

$$d(\mathbf{x}_L) + bias < z_L$$

- Take a weighted average of comparisons

# Shadow Maps

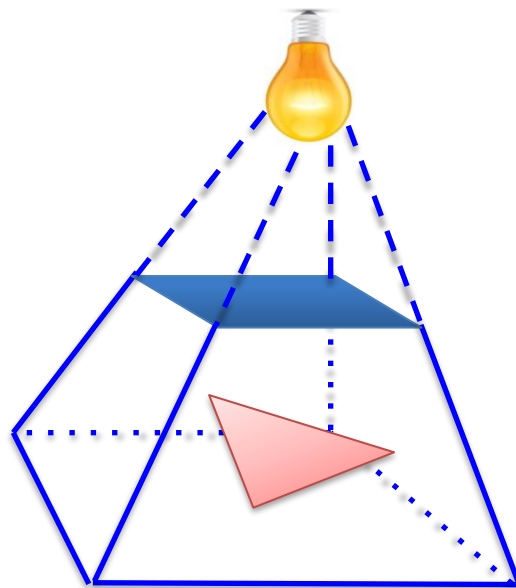
- Filtering
  - Take a weighted average of comparisons
  - Bigger filter produces fake soft shadows
  - Setting bias is tricky





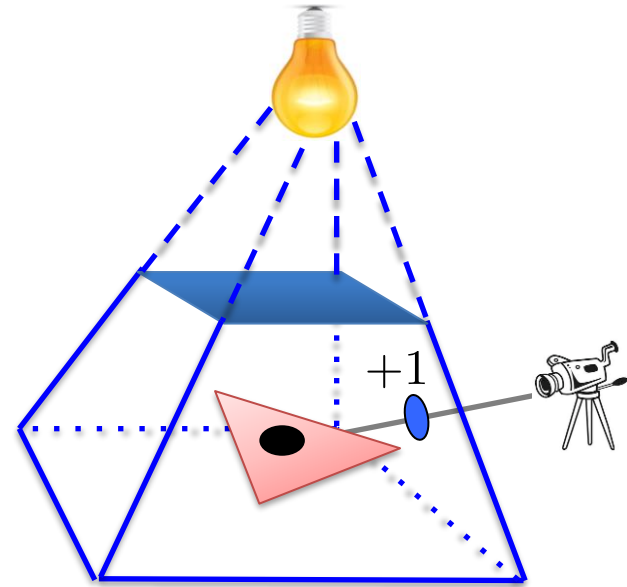
# Shadow Volumes

- Explicitly represent the volume of space in shadow
- If a polygon is inside the volume, it is in shadow
- Similar to clipping
- Naïve implementation:  
 $O(\#polygons \times \#lights)$



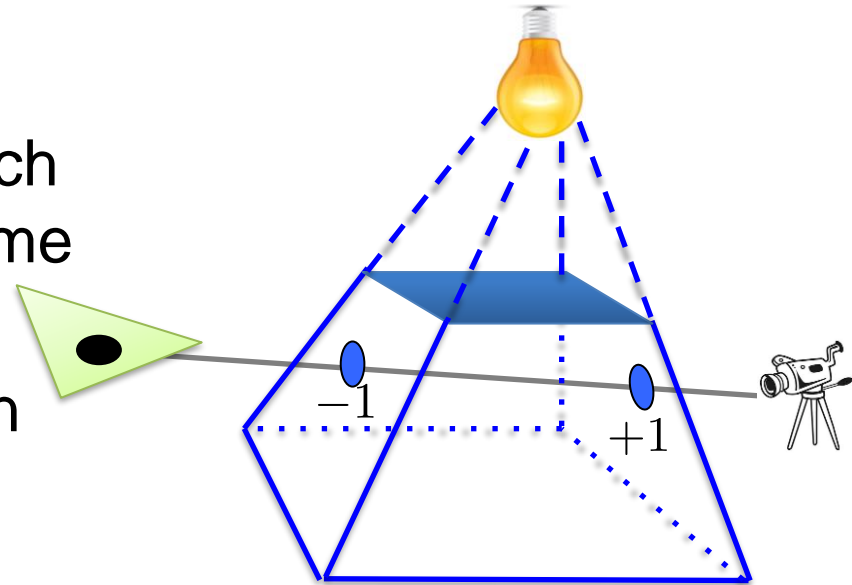
# Shadow Volumes

- Algorithm
  - Shoot a ray from the eye
  - Incre-/decrement a counter each time boundary of shadow volume is intersected
  - If counter  $> 0$ , primitive is in shadow



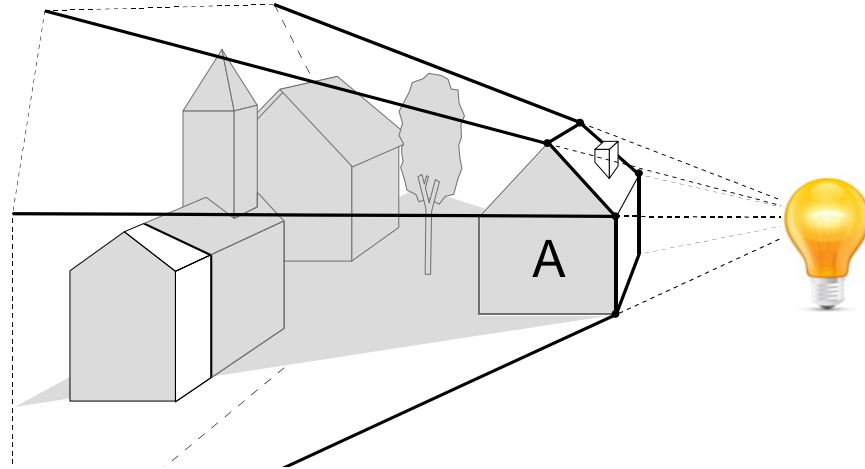
# Shadow Volumes

- Algorithm
  - Shoot a ray from the eye
  - Incre-/decrement a counter each time boundary of shadow volume is intersected
  - If counter = 0, primitive is not in shadow



# Shadow Volumes

- Optimization:
  - Use silhouette edges only  
(where a back-facing & front-facing polygon meet)



# Shadow Volumes

- Limitations
  - Introduces a lot of new geometry
  - Expensive to rasterize long skinny triangles
  - Objects must be watertight to use the silhouette optimization
  - Rasterization of polygons sharing an edge must not overlap & not have gap

# Comparisons

Features/Limitations	Planar Fake Shadows	Projective Texture Shadows	Shadow Maps	Shadow Volumes
Allows objects to cast shadows on themselves (self-shadowing)				
Permits shadows on arbitrary surfaces (i.e. curved)				
Generates extra geometric primitives				
Limited resolution of intermediate representation can result in jaggy shadow artifacts				